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Femtosecond laser irradiation of dielectric materials containing randomly-arranged nanoparticles

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ABSTRACT

We investigate femtosecond laser irradiation of dielectric materials containing randomly-arranged nanoparticles. For this, numerical modeling is performed based on three different methods: Mie theory, static solution of linear Maxwell's equations and a solution of nonlinear Maxwell's equations together with kinetic equations for free electron excitation/relaxation processes. First two approaches are used to define the static intensity distribution and to analyze the electromagnetic interaction between the nanoparticles. The third method allows us to investigate the complex dynamics of the laser-matter interaction. Multiphoton absorption is shown to be responsible for electron plasma generation in the regions of strong intensity enhancements in the vicinity of nanoparticles. The irradiation of the dielectric material leads to the elongation of nanoplasmas by the near-field enhancement perpendicular to the laser polarization and to their strong interaction resulting in periodic arrangement. Numerical results shed light on such effects as femtosecond laser-induced nanograting formation.

Keywords: Multiphoton absorption, femtosecond-laser interaction, transparent materials, nonlinear Maxwell's equations, Mie theory

1. INTRODUCTION

Femtosecond laser interactions have attracted increasing interest due to new possibilities for the efficient nanostructuring of different materials.¹⁻³ Nanoprocessing of transparent dielectrics is particularly promising since it enables writing optical waveguides, nanovoid arrays, polarization-dependent periodic surface structures and volume nanogratings.^{4,5} Recently, nanocomposites comprising metallic nanoparticles in a dielectric matrix have been shown to exhibit more pronounced nonlinear characteristics than the homogeneous transparent materials. These composites have already found a wide range of applications for solar cells, sensors and high-tech optical devices.⁶⁻¹⁰ In addition, periodic organization of nanostructures in transparent dielectrics containing metallic nanoparticles by ultrashort high-intensity laser irradiation has been evidenced in several recent works.¹¹⁻¹⁴ Furthermore, the doping elements in glasses were found to significantly improve the quality and the smoothness of the nanostructures and to facilitate the accumulation processes responsible for the self-organization.¹⁴⁻¹⁷

The optical response of metallic nanoparticles embedded in a dielectric matrix was studied in many works.¹⁸⁻²² The dipole-dipole interaction between polarized nanoparticles was found to be among possible sources of the composite optical nonlinearity. Particularly, it was shown that the impact of the dipole-dipole interaction increased with rise of nanoparticle concentration in the composite.²² Until now, the effect of the dipole-dipole interactions on the optical characteristics of the nanocomposites was mostly studied by the discrete dipole approximation for simulating clusters of spheres. It is worth noting that the coupled dipole method, being a linear approximation, is suitable only for weak optical fields. Moreover, the method disregards the transient properties of laser-irradiated glass.

When a high-intensity laser beam is tightly focused inside transparent dielectric, the properties of the material change considerably due to photoionization and avalanche effects.²³⁻²⁶ Furthermore, metallic nanoparticles embedded in glass matrix were shown to enhance nonlinear absorption during the laser structuring process.¹³ The scenario of nanoplasmas growth due to localized inhomogeneous nonlinear ionization was discussed in several pioneer works.²⁷⁻²⁹ In particular, the nanoplasmonics model based on the near-field enhancement at the tip of the

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nanoplasmas was proposed as the mechanism of the nanogratings formation in glass.²⁹ The generated electron plasma kinetics has been investigated in dielectrics in a few recent articles.^{30–35}

Herein, we discuss the dynamics of high-intensity ultrafast laser interaction with nanocomposites. We start by considering the optical response and the nonlinear interaction with one nanoparticle. Then, we investigate the collective response of a periodically-arranged nanoparticle array. Finally, we show the results for randomly distributed inclusions embedded in glass matrix.

2. NUMERICAL MODEL

In this paper, we use different methods to analyze the optical response of nanoparticles in glass. Method A and Method B provide static intensity distribution. Method C describes the complex dynamics of laser-matter interaction with nanoparticles in glass.

The first method (Method A) is an analytical static solution and is based on an approximation of the Mie solution.^{36,37} The scattered electric fields are calculated analytically for the case of a small $q \ll 1$ sphere in the near-field $kr \ll 1$ and in the far-field $kr \gg 1$ (see appendix). The total scattered field is the superposition of the fields scattered by each nanoparticle. The intensity corresponds to the square of the sum of the scattered and the incident fields. The approach describes the interference between the incident plane wave and the scattered field by homogeneous sub-wavelength spheres. The main advantage of this method is that we can separate dipole-dipole interaction from other types of more complex interactions as well as the response of each individual dipole from the interparticle dipole coupling. Unfortunately, the approach is applicable only for the inhomogeneities of special shape and limited size.

The second method (Method B) solves the linear Maxwell's equations using finite-difference time-domain (FDTD) method.³⁸ The method describes the intensity distribution at a fixed time of propagation and with a fixed density profile $n_e(x, z, t) = n_{e0}(x, z)$. This approach still allows us to separate the contribution of each electric field and, therefore, the incident field and the scattered field from the total field. The method solves only static problems. Additionally, even at the fixed time, it is not precise because of the difficulty to define exactly the density profiles evolving in the study.

Finally, the third method (Method C) is based on the nonlinear Maxwell's equations coupled with electron density equation. The kinetics of the electron plasma in the transparent material is described, as follows

$$\begin{cases} \frac{\partial \vec{E}}{\partial t} = \frac{\nabla \times \vec{H}}{\epsilon_0} - \frac{1}{\epsilon_0} \vec{J}_{nl} \\ \frac{\partial \vec{H}}{\partial t} = -\frac{\nabla \times \vec{E}}{\mu_0} \\ \frac{\partial n_e}{\partial t} = (n_a - n_e)w_{pi} - \frac{n_e}{\tau_{tr}}, \end{cases} \quad (1)$$

where \vec{E} is the electric field, \vec{H} is the magnetic field, \vec{J}_{nl} is the nonlinear current consisting of two parts, the first term derived from the Drude model for the dispersive media with time-dependent electron density n_e and the second photoionization term considering a complete Keldysh photoionization rate w_{pi} .³⁹ Free carrier number density changes due to photoionization w_{pi} and recombination effect with $\tau_{tr} = 150$ fs.⁴⁰ The electromagnetic response of the metallic nanoparticles is calculated from the linear Maxwell's equations with the current term derived from the Drude-Lorentz model for gold.⁴¹ In this method, we consider initial Gaussian electric field profile and Gaussian temporal envelope. The details of the numerical model and modeling parameters for glass can be found in Ref. [35]. This method is able to follow the kinetics of electron plasma generated in the near field of the embedded nanoparticles. However, the method does not allow us to separate linear and nonlinear processes and to elucidate which interaction is responsible for the nanoplasmas growth and interaction.

We note, that all the resulting snapshots of the electric fields, intensity and electron density are in the plane xOz , where the light is polarized along x direction and z is the propagation direction.

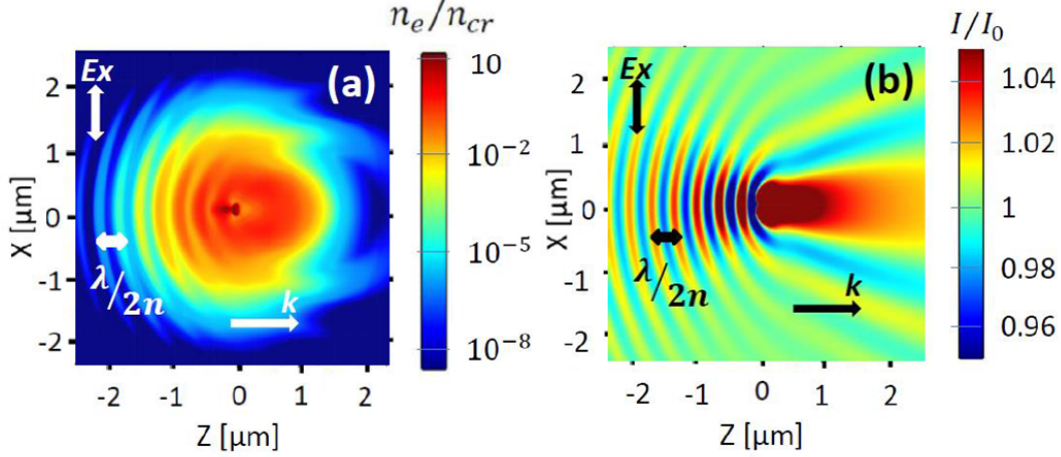


Figure 1. (a) Electron density distribution is calculated by 2D-Maxwell's equations coupled with electron density equation (Method C) at the peak of 80 fs laser pulse irradiating a single nanoparticle; (b) Static analytical Mie theory intensity distribution (Method A) for a small nanoparticle of radius $a = 5$ nm localized in (0,0) (interference between the incident plane wave and the scattered spherical wave). Here, laser irradiation conditions: pulse duration $\theta = 80$ fs (FWHM), irradiation wavelength in air $\lambda = 800$ nm, pulse energy $E = 300$ nJ. Electron density is normalized to its critical value at 800 nm $n_{cr} = 1.7 \times 10^{27} m^{-3}$ and \vec{k} is the incident laser wave vector.

3. RESULTS AND DISCUSSION

First, we consider the optical response of one nanoparticle embedded in glass. The intensity in the near-field of the gold nanoparticle is strongly enhanced in the polarization direction and leads to the organization of electron plasma (non visible in Fig. 1(a)).^{33,35,42} The interference between the incident and the scattered far-field spherical wave leads to the organization of periodical minima and maxima in the direction of the light propagation (Fig. 1(a,b)). This phenomenon can be explained by considering the dipole approximation method (Method A). The scattered electric field $E_x^{(s)} \propto E_\theta^{(s)} \propto B_1^e \frac{\exp(ikz)}{kz}$ interferes with the incident polarization field $E_x^{(i)} \propto \exp(-ikz)$ (see appendix). Fig. 1(b) shows that the interference results in the organization of the standing wave with the intensity distribution $I \propto \frac{\exp(2ikz)}{(kz)^2}$ having maxima and minima separated by $\Delta z = \lambda/2n$. The dynamics of the interaction of the laser light with plasma is defined by this strong enhancement in the direction backward to the laser propagation.

Second, we study the interaction of the organized nanoplasmas from several nanoparticles embedded in glass (Fig. 2). The mutual enhancement induced by the plasma interaction strongly depends on the distance between the initial nanoparticles. The optical response of the ensemble is the sum of the individual nanoplasma contributions modified by interparticle coupling that depends on specific geometry and, therefore, on the initial particle localization. Fig. 2(a) shows that for widely separated nanoparticles, the behavior is independent. Hence, the interference between the incident and the scattered field dominates over plasmonic modes.⁴³ At closer distance, the interparticle coupling starts playing a role. We can see periodically organized patterns between the nanoplasmas corresponding to the mutual enhancements in Fig. 2(b,c). The closer the nanoplasmas are, the stronger their collective response.²² It is worth noting that the approximation method A cannot be applied in the case of closely separated nanoparticles with $kr \approx 1$. Thus, it is inapplicable for nanoparticles with interparticle separation significantly less than the irradiation wavelength in medium. The method B solving the complete system of Maxwell's equations should be used to understand the interaction of nanoplasmas in close proximity.

In the cases of one nanoparticle and widely separated nanoparticles embedded in glass, the resulting intensity distribution was defined mostly by the $E_x^{(s)} \propto E_\theta^{(s)} \propto B_1^e \frac{\exp(ikz)}{kz}$ electric field component, where B_1^e is the first electric dipole moment (see appendix). The contribution of $E_r^{(s)} \propto B_1^e \frac{\exp(ikr)}{(kr)^2}$ is roughly negligible as it decreases very fast in the radial direction. However, for metallic nanoparticles, the magnetic moment is of the same order as

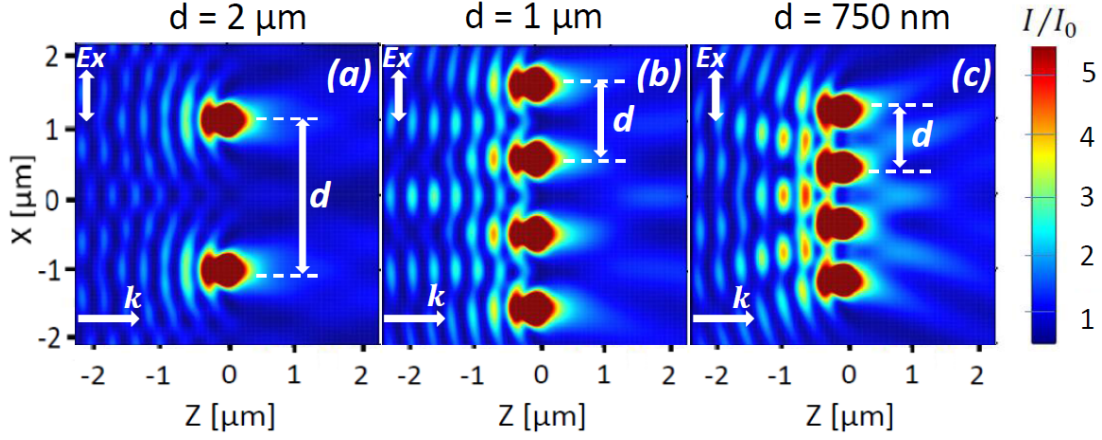


Figure 2. Static analytical Mie theory intensity distribution (Method A) for small nanoparticles of radius $a = 50$ nm with interparticle separations a) $d = 2\mu\text{m}$ b) $d = 1\mu\text{m}$ c) $d = 750\text{nm}$ (interference between the incident plane wave and the scattered spherical wave). Laser irradiation wavelength is $\lambda = 800$ nm in air.

the dipole moment order (see appendix).^{37,44} The orthogonal scattered field in the first approximation is defined as $E_z^{(s)} \propto E_\theta^{(s)} \propto B_1^m \frac{\exp(ikr)}{kr}$, where B_1^m is the first magnetic dipole moment. The contribution of this field influences strongly the resulting intensity distribution. In the next paragraph we investigate the contribution of the orthogonal field.

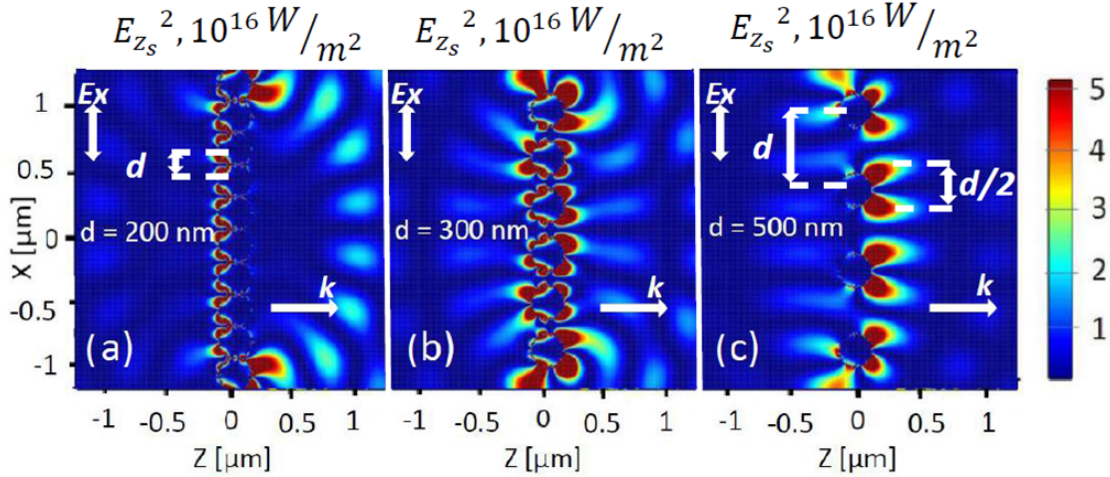


Figure 3. Multiple scattering intensity distributions for a periodic array of nanoparticles of radius $a = 100$ nm with different interparticle separations: (a) $d = 200$ nm, (b) $d = 300$ nm, (c) $d = 500$ nm are calculated by linear Maxwell's equations (Method B). Laser irradiation wavelength is $\lambda = 800$ nm in air.

In what follows, we analyze the character of multiple scattering induced by the orthogonal field from closely arranged nanoparticles (Fig. 3). An array of periodic high density spherical nanoparticles with radius $a = 100$ nm is illuminated simultaneously by a plane wave. We vary the interparticle separation distance d and study the resulting intensity distribution calculated by linear Maxwell's equations (Method B). For particle dimensions much smaller than the wavelength, interference effect is negligible but interparticle coupling becomes significant. For nearly touching nanoparticles, plasmons exhibit multipolar behavior,⁴⁵ including a very high local concentration of electromagnetic energy in the vicinity of their conductive contact Fig. 3(a). In this

case, the scattering patterns depend strongly on the particle size and, correspondingly, on the interparticle separation. Therefore, the period of the interference patterns due to multiple scattering is directly proportional to the interparticle separation. However, the near-field enhancement might have nontrivial distribution when the interparticle coupling effects take place.^{46,47} Fig. 3(b) demonstrates that as d grows, the periodicity of enhancements also changes. For distances longer than the nanoparticle size, the character of scattering is qualitatively different and the periodicity is about half the interparticle separation in Fig. 3(c). It is worth noting that the intensity enhancement induced in the near-field of the closely spaced nanoparticles by the orthogonal field might considerably change the electron density distribution and the direction in which the nanoplasmas grow.

We have investigated the role of both components of the electric field in the case of periodically arranged nanoparticles without taking into account the transient properties of the dielectric material. We note, that such a physical interpretation can be considered only as a very rough approximation of the complex studying problem where the size and the density of nanoplasmas change in time. Hence, we perform FDTD calculations based on solution of the system of coupled equations (Method C) with initially periodically arranged nanoparticles (Fig. 4). Interestingly, the electron density snapshots taken before the pulse peak already show two regimes with different scattering behavior for different initial interparticle separations. In both cases, the nanoplasmas elongate from the nanoparticles in the backward propagation direction. For the nanoparticles in close proximity, the nanoplasmas merge together organizing the nanoplanes with exact periodicity of the initial interparticle separation in Fig. 4(a). At larger separation distances, each nanoplasma is divided into two and the final periodicity is half the interparticle separation in Fig. 4(b). In fact, such behavior can be explained by the intensity enhancements induced by the orthogonal field and calculated by linear Maxwell's equations in Fig. 3(c). The nanoplasmas always grow into the direction where the intensity is strongly enhanced.

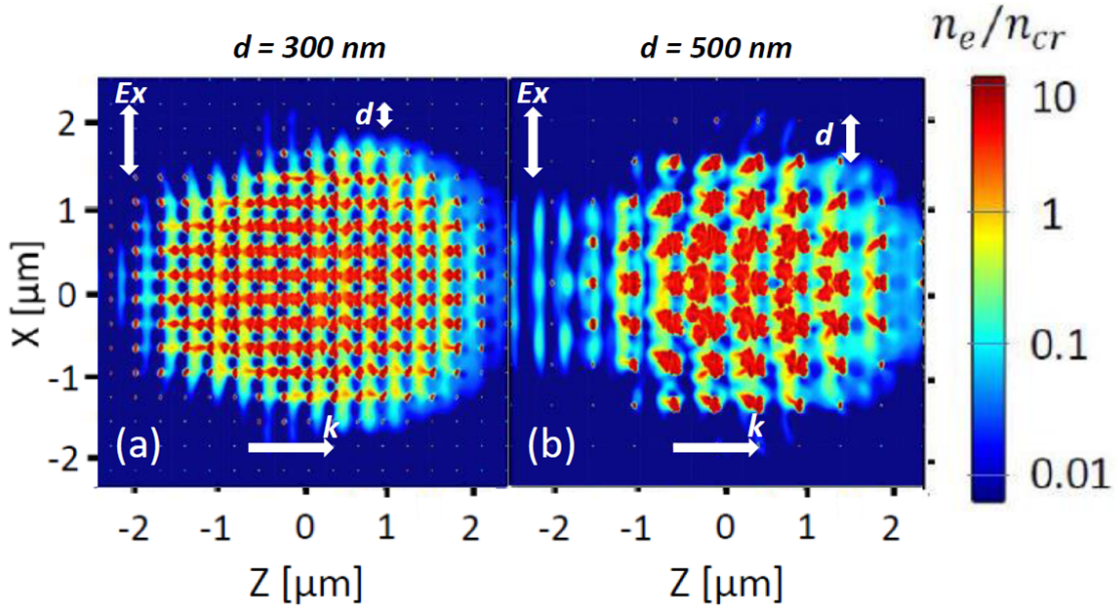


Figure 4. Electron density snapshots calculated by 2D-Maxwell's equations coupled with electron density equation (Method C) 40 fs before the pulse peak. Laser irradiation conditions: pulse duration $\theta = 240$ fs (FWHM), irradiation wavelength in air $\lambda = 800$ nm, pulse energy $E = 500$ nJ. Electron density is normalized to its critical value at 800 nm $n_{cr} = 1.7 \times 10^{27} m^{-3}$. The interparticle separation is (a) $d = 300$ nm, (b) $d = 500$ nm.

Finally, the calculation results using nonlinear Maxwell's equations coupled with free electron density equation (Method C) for glass with initial randomly distributed nanoparticles are shown in Fig. 5. The first snapshot in Fig. 5(a) taken far before the peak pulse shows that each nanoparticle exhibits dipole behavior in the near-field and in the far-field. The interference of the incident and the scattered spherical waves from nanoparticles induces periodic strong enhancements backwards to the laser propagation. As a result, the nanoplasmas are elongated

perpendicular to the laser propagation in Fig. 5(b). They strongly interact with each other. The nanoplasmas in close proximity merge together, slightly changing their direction. Fig. 5(c) shows that the mutual interaction leads to organization of quasi-periodic nanoplasma planes perpendicular to the laser polarization. Previously, it was reported that femtosecond laser irradiation of fused silica bulk might lead to the self-organization of nanogratings consisting of high density plasma.^{13, 29, 42, 48, 49} Small inhomogeneities are required to initiate the process.³³ Here, we show that the nanoparticles can also play the same role of seeds for the nanoplasmas. Moreover, we underline that the self-organization of final structures can be explained by the electromagnetic approach coupled with the electron density equation to describe the dynamics of femtosecond laser interaction with dielectric materials.

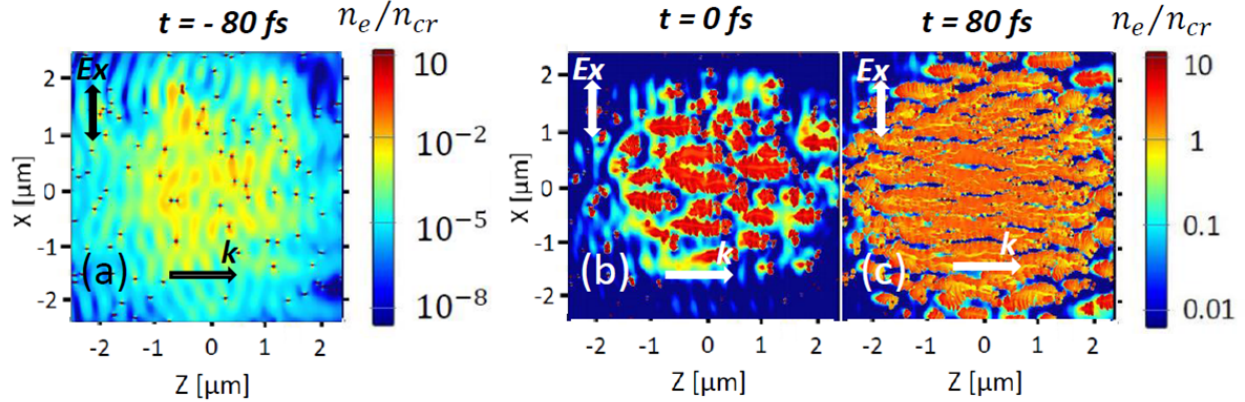


Figure 5. Electron density snapshots are calculated by 2D-Maxwell's equations coupled with electron density equation (Method C) revealing the evolution of nanogratings (a) 80 fs before the pulse peak, (b) at the pulse peak, (c) 80 fs after the pulse peak. Laser irradiation conditions: pulse duration $\theta = 240$ fs (FWHM), irradiation wavelength in air $\lambda = 800$ nm, pulse energy $E = 500$ nJ. Electron density is normalized to its critical value at 800 nm $n_{cr} = 1.7 \times 10^{27} m^{-3}$. The average initial interparticle distance is $d = 400$ nm. In Fig. 5(a) the scale is different than in Fig. 5(b) and in Fig. 5(c).

4. CONCLUSION

We have investigated ultrashort laser interaction with dielectric materials containing randomly-arranged nanoparticles. Three methods have been applied to explain the optical response of the quasi-metallic nanoplasma organized due to enhanced nonlinear absorption in the vicinity of the embedded nanoparticles: analytical solution from Mie theory (Method A), linear Maxwell's equations (Method B) and nonlinear Maxwell's equations coupled with electron density equation (Method C).

1) It is shown that the dipole approximation method can explain the near-field enhancement at the tip of nanoplasma resulting in nanoplasma growth.

2) The distance between the randomly elongated nanoplasmas should be at least less than the irradiation wavelength in glass, otherwise, the mutual enhancement is negligible. This distance allows us to estimate the initial concentration of the embedded nanoparticles which is required for significant near-field enhancement.

3) At closer nanoplasma separation, the mutual interaction exhibits complex behavior. Particularly, the contribution of the orthogonal field for the closely arranged metallic nanoparticles is not negligible. The intensity enhancement induced by the orthogonal field might considerably change the electron density distribution and the direction in which the nanoplasmas grow.

4) The results of calculations show that the nanoparticles act like reservoirs of available electrons,¹³ inducing the formation of long nanoplasmas. The nanoplasmas mutually interact and are arranged in quasi-periodic planes perpendicular to the laser polarization.

4.1 Appendix

The electric fields scattered by homogeneous sphere in spherical coordinates (r, θ, ϕ) can be written as follows^{36,37}

$$\begin{cases} E_r^{(s)} = \frac{\cos\phi}{k^2 r^2} \sum_{l=1}^{\infty} l(l+1) B_l^e \varsigma_l^{(1)}(kr) P_l^{(1)}(\cos\theta) \\ E_\theta^{(s)} = -\frac{\cos\phi}{kr} \sum_{l=1}^{\infty} \left(B_l^e \varsigma_l^{(1)'}(kr) P_l^{(1)'}(\cos\theta) \sin\theta - i B_l^m \varsigma_l^{(1)}(kr) P_l^{(1)}(\cos\theta) \frac{1}{\sin\theta} \right) \\ E_\phi^{(s)} = -\frac{\sin\phi}{kr} \sum_{l=1}^{\infty} \left(B_l^e \varsigma_l^{(1)'}(kr) P_l^{(1)}(\cos\theta) \frac{1}{\sin\theta} - i B_l^m \varsigma_l^{(1)}(kr) P_l^{(1)'}(\cos\theta) \sin\theta \right), \end{cases} \quad (2)$$

where B_l^e and B_l^m are electric and magnetic dipole moments, k is the wave vector in the medium, $\varsigma_l^{(1)}(kr)$ are the spherical Henkel functions of the first kind, and $P_l^{(1)}(\cos\theta)$ are Legendre polynomials of the first kind. Additionally, the fields have a time dependence factor $\exp(-i\omega t)$ that has been suppressed in the above equations.

The asymptotes for Henkel functions are as follows

- i) Near-field ($kr \ll 1$): $\varsigma_1^{(1)}(kr) = -\frac{i}{kr}$ and $\varsigma_1^{(1)'}(kr) = \frac{i}{(kr)^2}$.
- ii) Far-field ($kr \gg 1$): $\varsigma_1^{(1)}(kr) = -\exp(ikr)$ and $\varsigma_1^{(1)'}(kr) = -i \cdot \exp(ikr)$.

Small size approximations ($q \ll 1, nq \ll 1, l = 1$): $B_1^e = iq^3 \frac{n^2-1}{n^2+2}$, $B_1^m = iq^5 \frac{n^2-1}{30}$, $B_l^e \rightarrow 0$, $B_l^m \rightarrow 0$, $l > 1$.

For small metallic nanoparticle ($q \ll 1, nq \gg 1, l = 1$): $B_1^e = iq^3$, $B_1^m = i\frac{q^3}{2}$, $B_l^e \rightarrow 0$, $B_l^m \rightarrow 0$, $l > 1$.

Legendre polynomials for $l = 1$: $P_1^{(1)}(\cos\theta) = \sin\theta$ and $P_1^{(1)'}(\cos\theta) = -\frac{\cos\theta}{\sin\theta}$.

The scattered electric fields in Cartesian coordinate system:

$$\begin{cases} E_x^{(s)} = E_r^{(s)} \sin\theta \cos\phi + E_\theta^{(s)} \cos\theta \cos\phi - E_\phi^{(s)} \sin\phi \\ E_y^{(s)} = E_r^{(s)} \sin\theta \sin\phi + E_\theta^{(s)} \cos\theta \sin\phi + E_\phi^{(s)} \cos\phi \\ E_z^{(s)} = E_r^{(s)} \cos\theta - E_\theta^{(s)} \sin\theta. \end{cases} \quad (3)$$

4.2 Acknowledgments

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